

Visual Medicine: Part Two – Advanced Topics in Visual Medicine



Diffusion Tensor Imaging

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DT-MRI



Measurement basics

Understanding Tensor Shape

Data Inspection with Glyphs

Fiber Tracking and Analysis

Future Work Ideas

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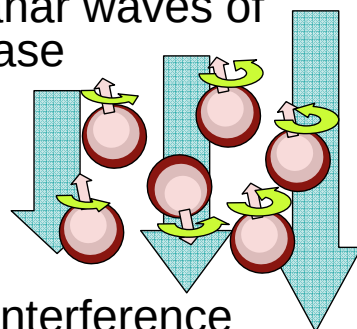
Future Work Ideas

Diffusion-weighted MRI (DW-MRI)

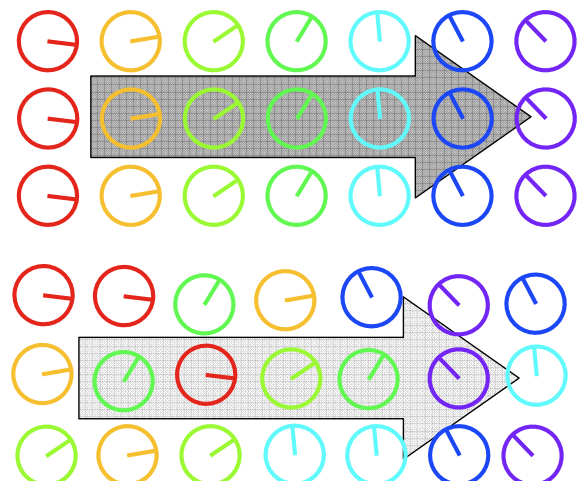
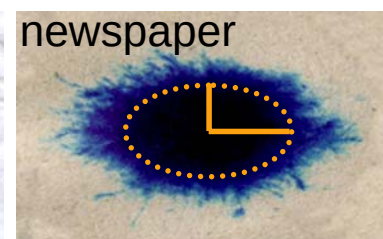
Brownian motion of one material through another

Anisotropy: diffusion rate depends on direction

Magnetic gradients create spatial planar waves of proton phase

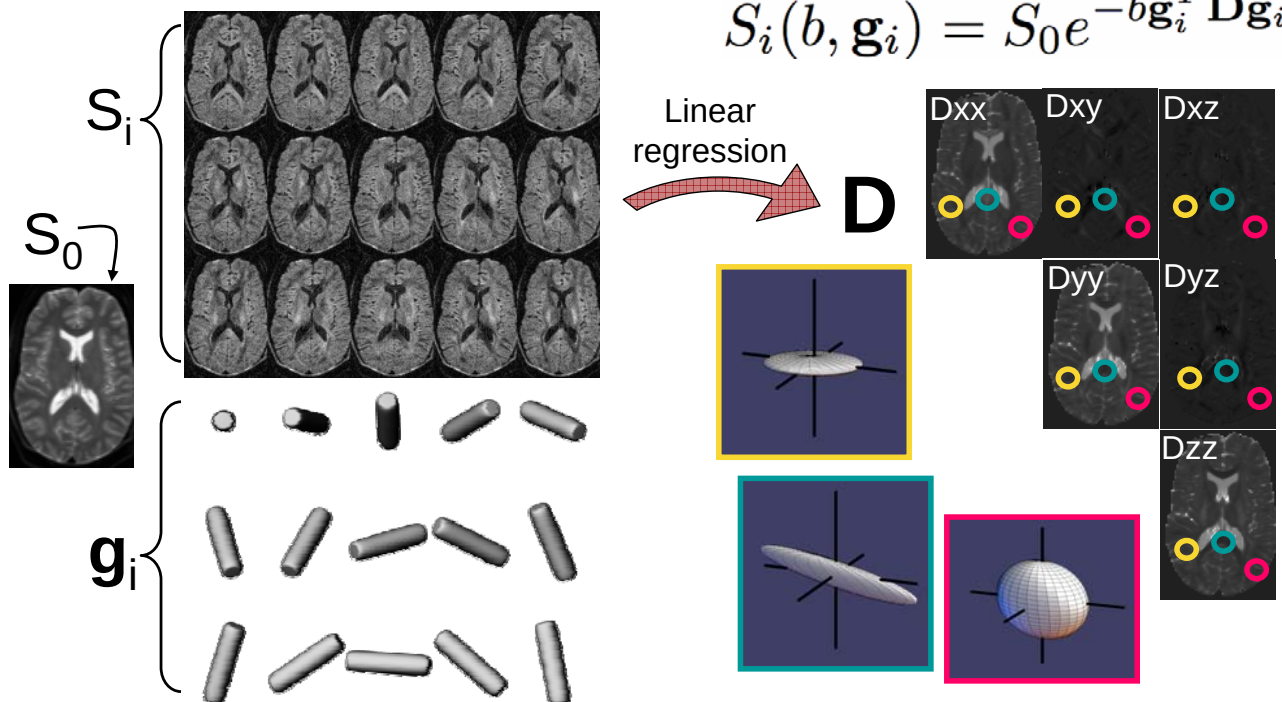


Destructive interference measures diffusion along gradient direction only

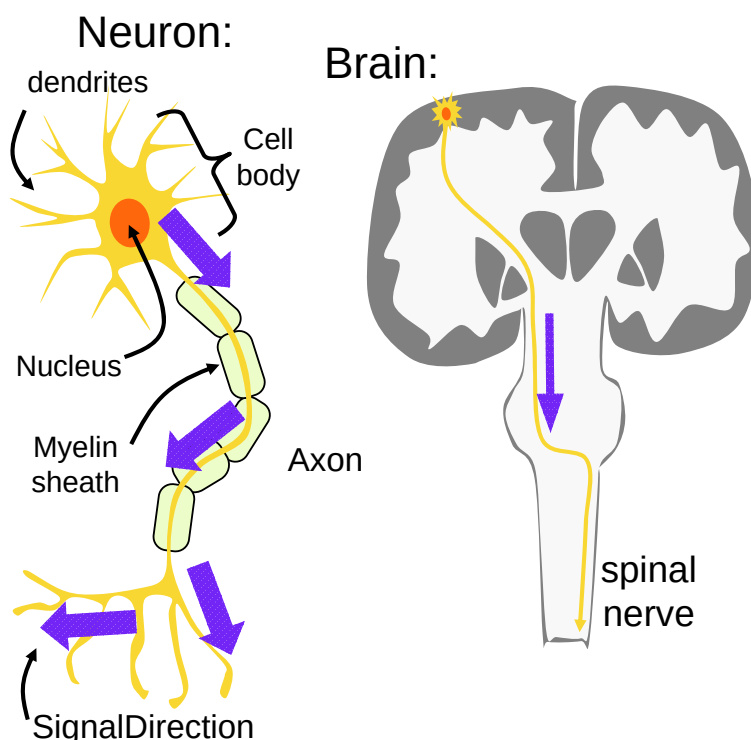


Multiple DWI → Tensor Estimate

Single Tensor Model (Basser 1994)



Underlying Biology



Gray matter (cortex + nuclei): cell bodies

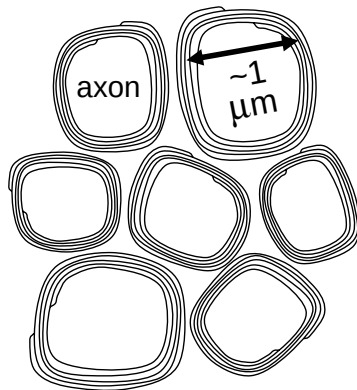
White matter: axons

Myelin sheath aids signal conduction

Axon + sheath = nerve fibers

Major white matter pathways aggregate many fibers into bundles

Cross-section:



Microstructure of bundles directionally constrains water diffusion along fiber direction (LeBihan et al. 1985)

Intra- and extra-cellular diffusion

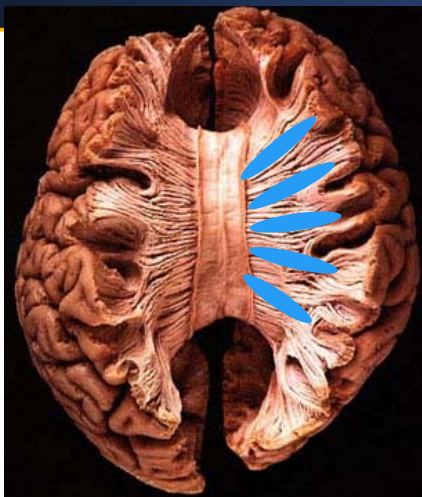
Diffusion lengths with the time-scale of MR measurement ($TE \approx 100\text{ms}$) on order of $10\mu\text{m}$

Apparent diffusion coefficient: ADC

Voxels on the order of 1mm

⇒ Roughly two orders of magnitude away from measuring axons

Applications



Images from Virtual Hospital (www.vh.org)

- Neuroanatomy
- Neurosurgery: tumor/tract relationship
- Stroke: detection
- Degenerative diseases: ALS, Multiple Sclerosis
- Psychiatric disorders: Schizophrenia

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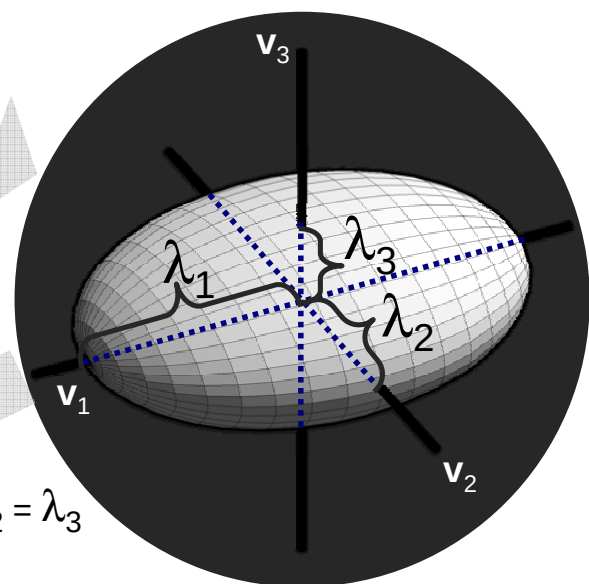
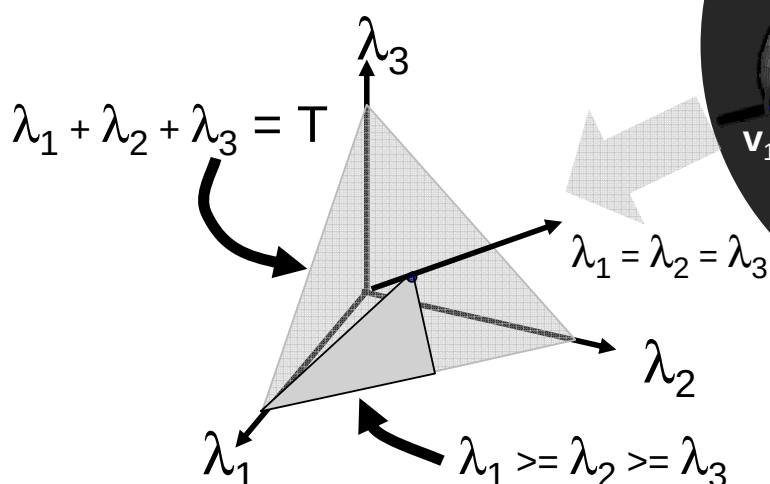
Fiber Tracking and Analysis

Future Work Ideas

Eigenvalues == Shape

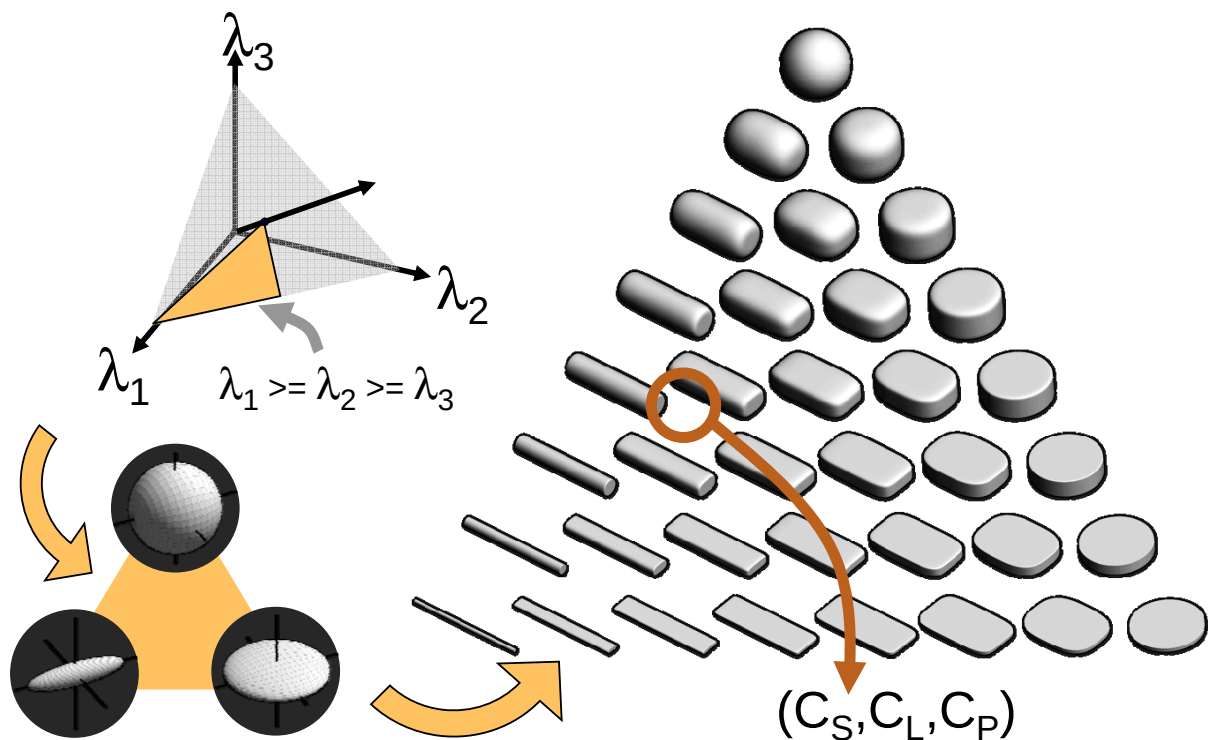
$$\mathbf{D} = \mathbf{R} \mathbf{\Lambda} \mathbf{R}^{-1}$$

$$= \begin{bmatrix} | & | & | \\ \mathbf{v}_1 & \mathbf{v}_2 & \mathbf{v}_3 \\ | & | & | \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \begin{bmatrix} -\mathbf{v}_1 \\ -\mathbf{v}_2 \\ -\mathbf{v}_3 \end{bmatrix}$$



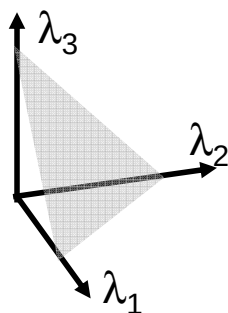
Tensor shape always
has 3 degrees of freedom

Barycentric shape space



Tensor invariants as orthogonal shape parameterizations

Cylindrical or spherical coordinates
(Ennis+Kindlmann 2005)

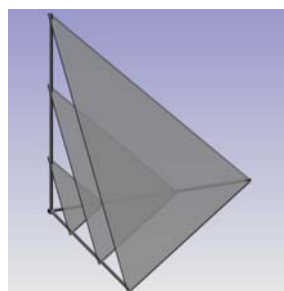


$$\text{tr}(\mathbf{D}) = D_{xx} + D_{yy} + D_{zz}$$

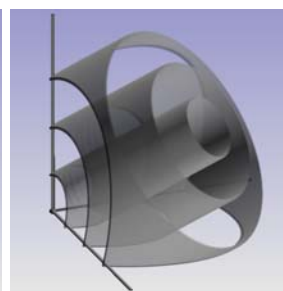
$$|\mathbf{D}| = \sqrt{\text{tr}(\mathbf{D}^T \mathbf{D})}$$

$$\mathbf{E} = \text{deviatoric}(\mathbf{D})$$

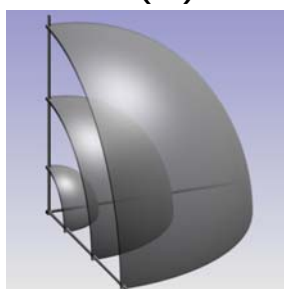
$$= \mathbf{D} - \text{trace}(\mathbf{D}) \cdot \mathbf{I} / 3$$



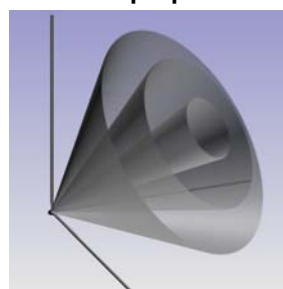
$\text{tr}(\mathbf{D})$



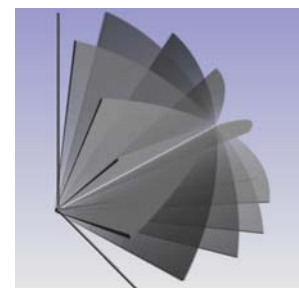
$|\mathbf{E}|$



$|\mathbf{D}|$



$|\mathbf{E}|/|\mathbf{D}|$
 $= \sqrt{2/3} \text{ FA}$

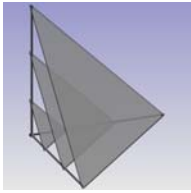


$\text{mode}(\mathbf{E})$
 $= \det(\mathbf{E}/|\mathbf{E}|)$
(Criscione '00)
Mode measures
Linear vs. planar
anisotropy

Biological Significance of Tensor Shape

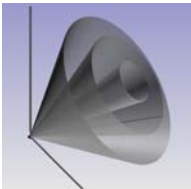


Size: bulk mean diffusivity (“ADC”)



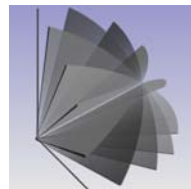
- ADC strictly speaking diffusivity along **one** direction
- $\text{tr}(\mathbf{D})$ same across gray+white matter, high in CSF
- Indicator of acute ischemic stroke

Anisotropy (e.g. FA, RA): directional microstructure



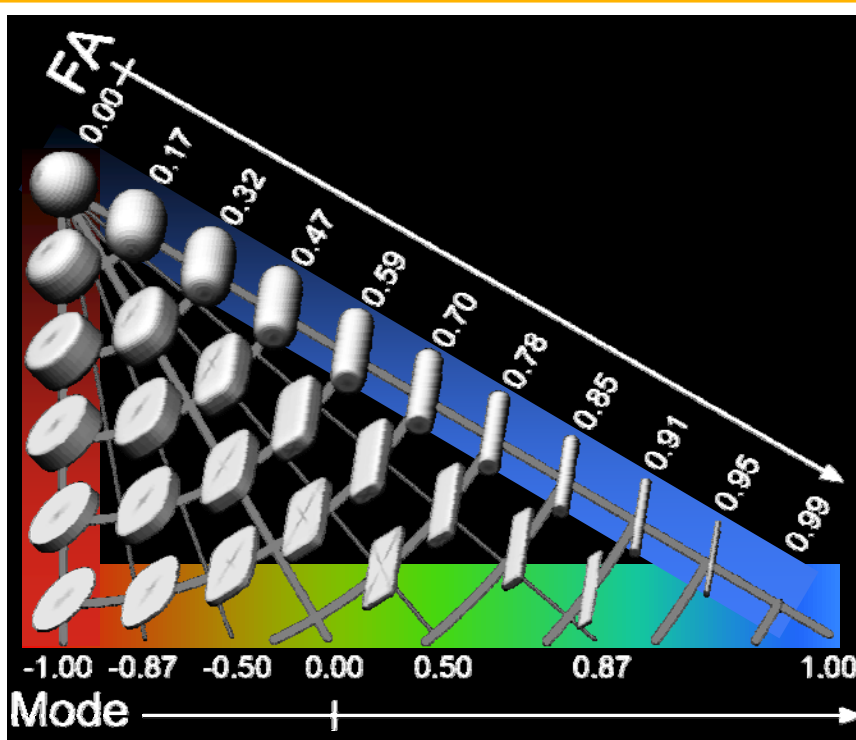
- High in white matter, low in gray matter and CSF
- Increases with myelination, decreases in some diseases

Mode: linear versus planar



- Partial voluming of adjacent orthogonal structures
- Fine-scale mixing (superior longitudinal fasciculus)
- Tensor fitting error increases with planarity (Tuch 2002)

Orthogonal vs. barycentric invariants



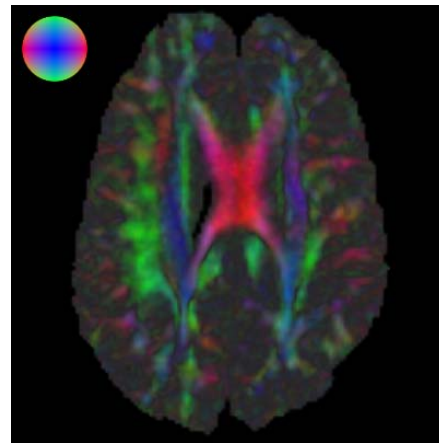
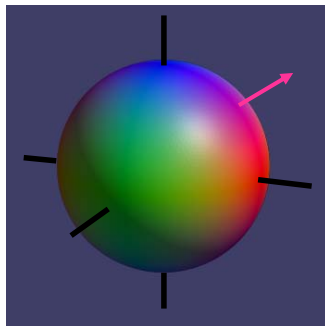
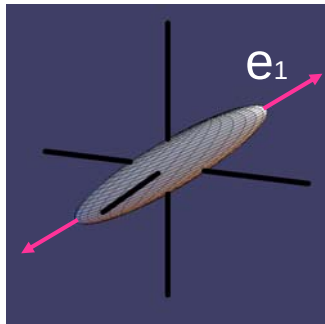
High FA $\Rightarrow$ linear
ONLY when FA >
 $1/\sqrt{2}$

Need both FA and
mode to
characterize high
linear anisotropy

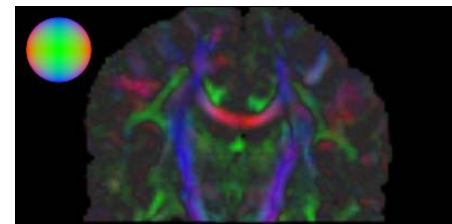
$|\mathbf{D}|$ constant

Significance of Tensor Orientation

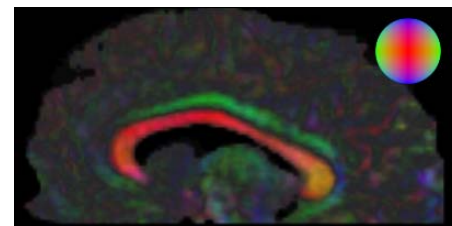
Principal eigenvector gives axon bundle direction



Axial



Coronal



Sagittal

$$\begin{aligned} R &= | \mathbf{e}_1 \cdot \mathbf{x} | \\ G &= | \mathbf{e}_1 \cdot \mathbf{y} | \\ B &= | \mathbf{e}_1 \cdot \mathbf{z} | \end{aligned} \quad (\text{Pierpaoli et al., 1997})$$

(demo of
colormaps)

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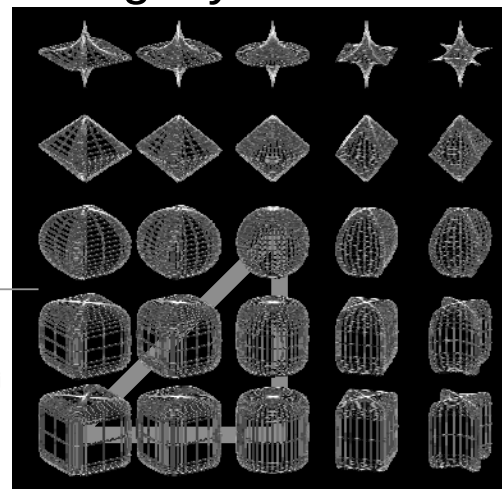
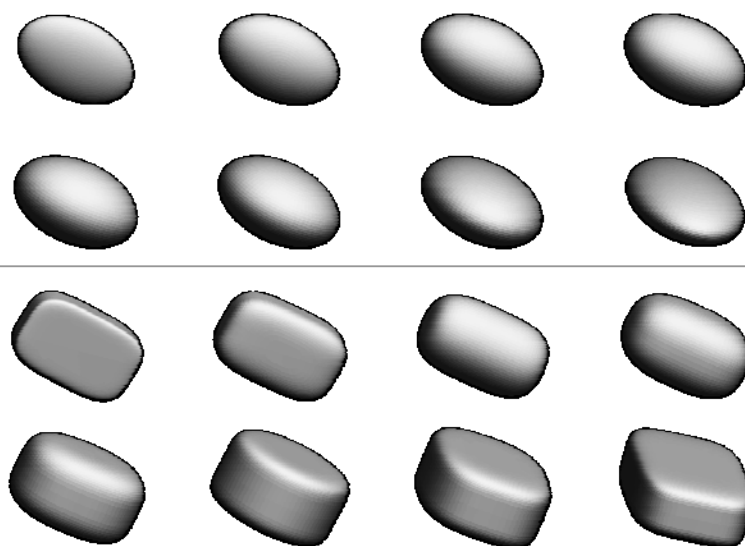
Fiber Tracking and Analysis

Future Work Ideas

Glyphs for inspecting tensors

Superquadric tensor glyphs (Kindlmann 2004)

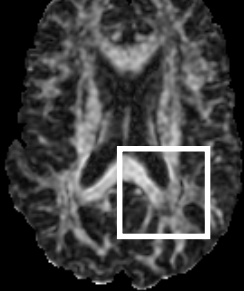
- Avoids visual (“bas-relief”) ambiguity



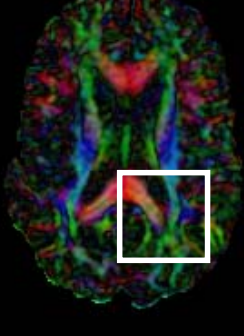
(Barr 1981)



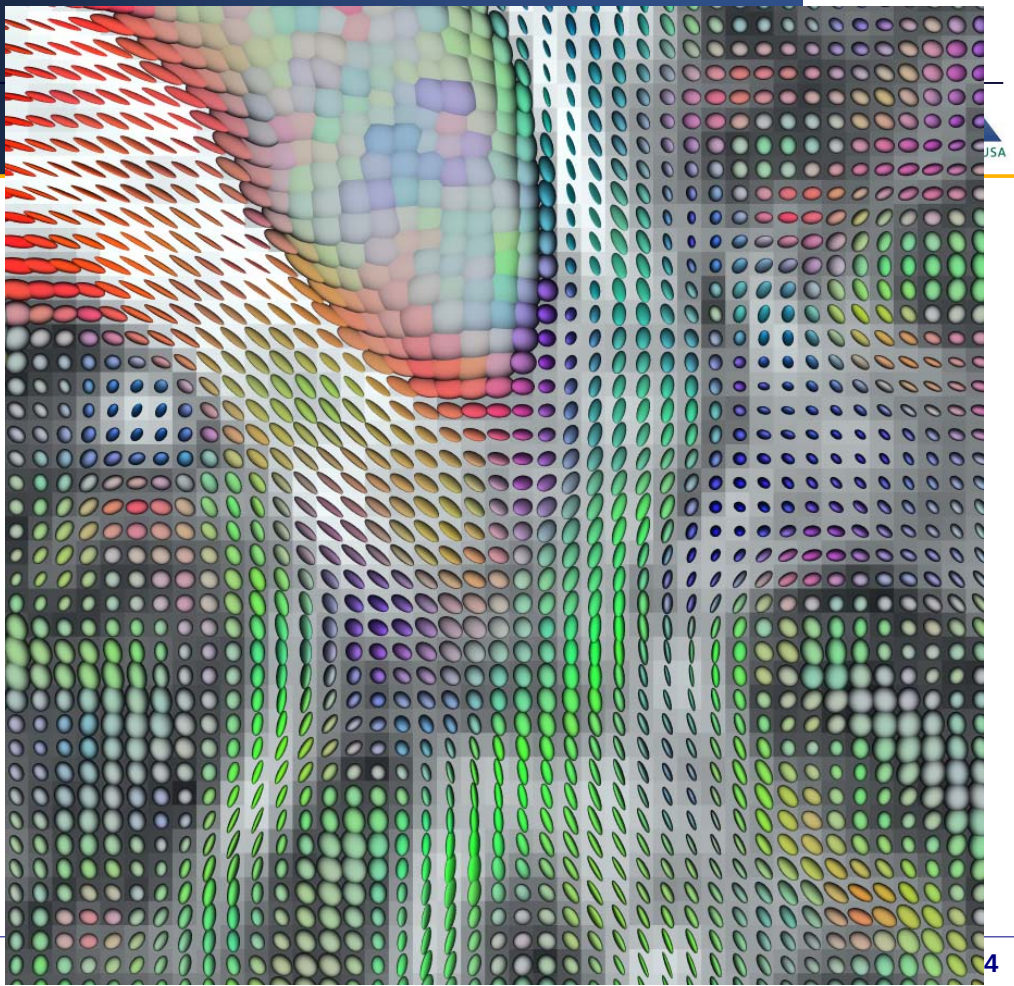
Backdrop: FA



Color: RGB(e_1)



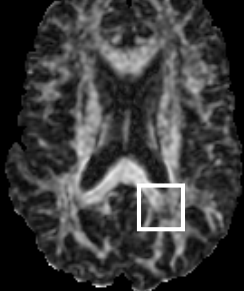
IEEE Visualization 2006



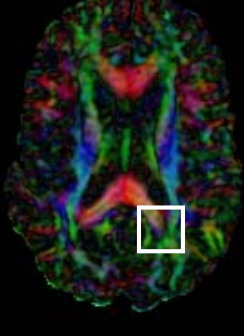
4



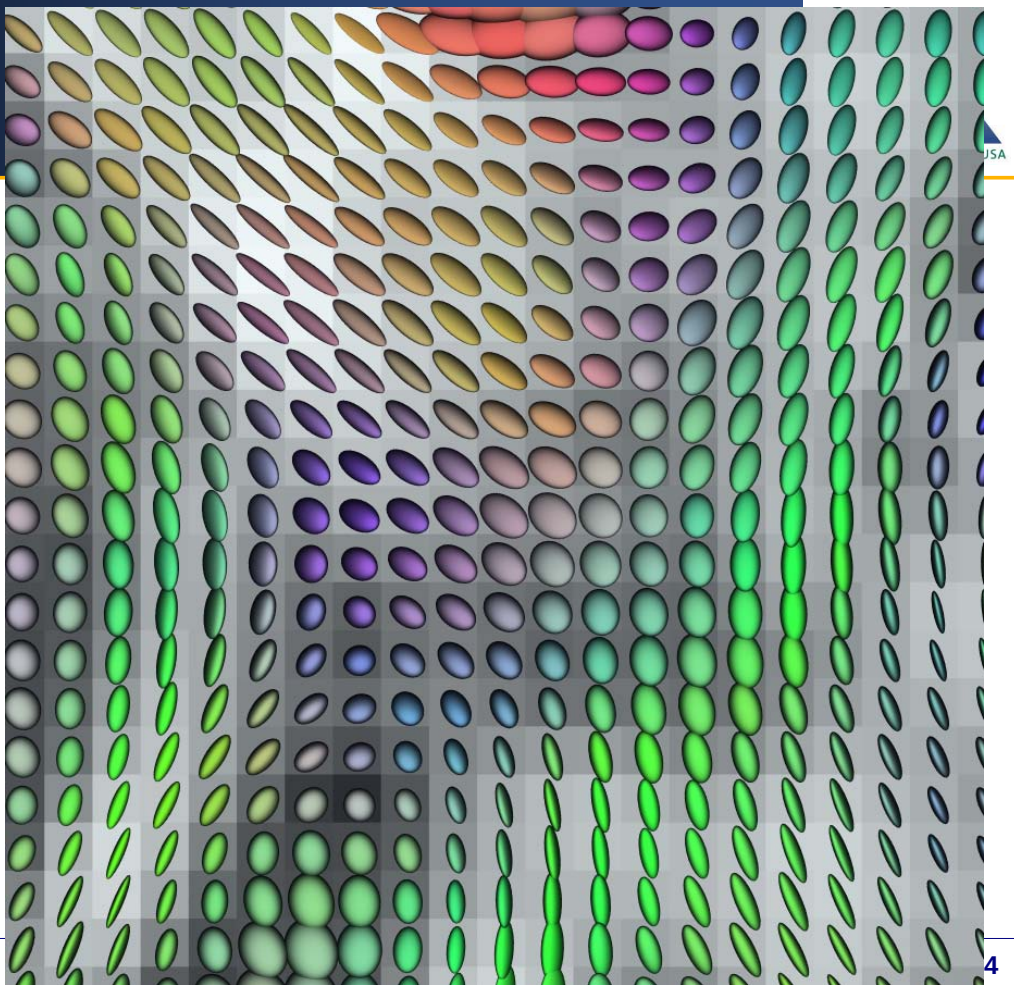
Backdrop: FA



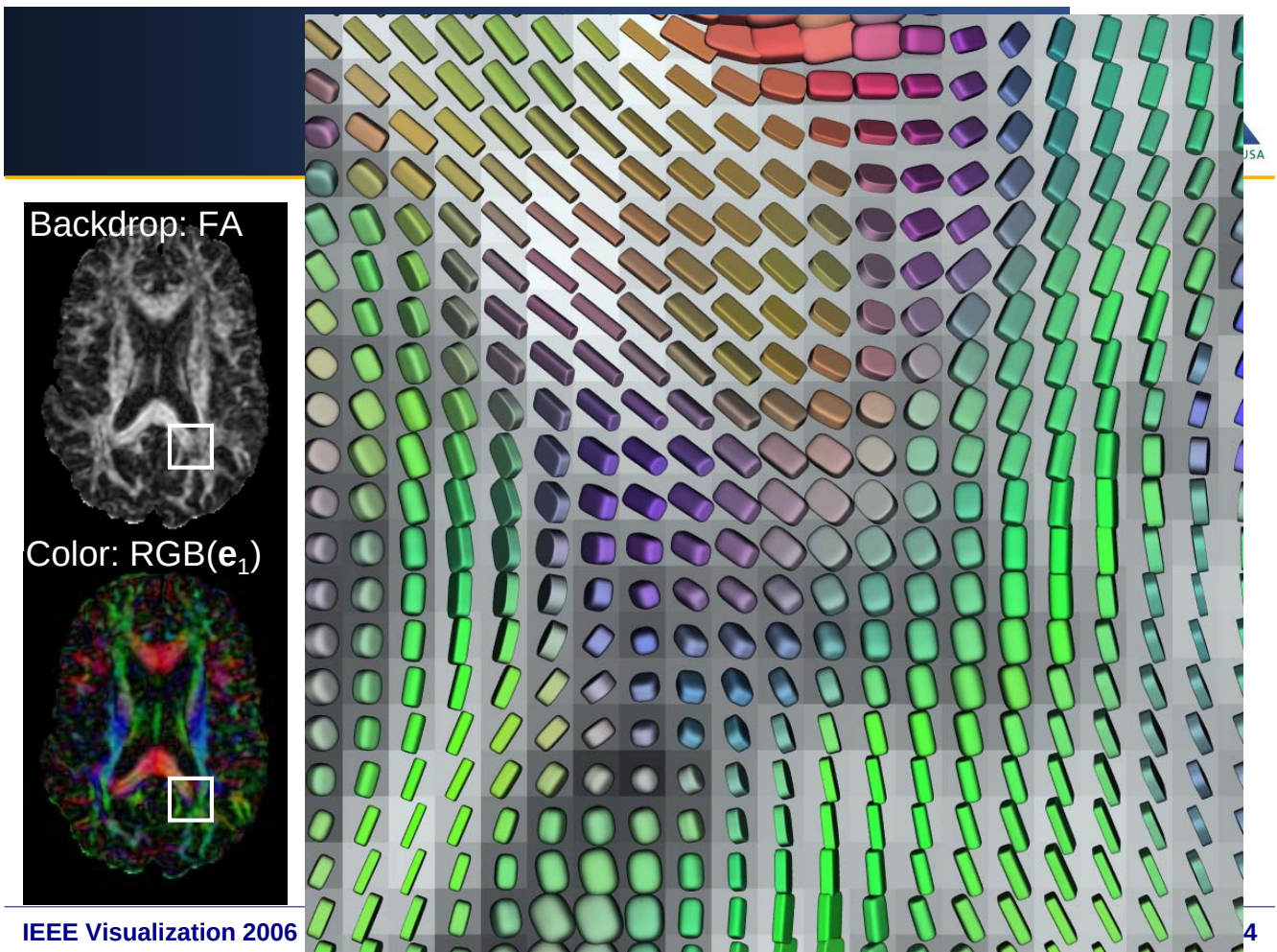
Color: RGB(e_1)



IEEE Visualization 2006



4



Particle systems for glyphs

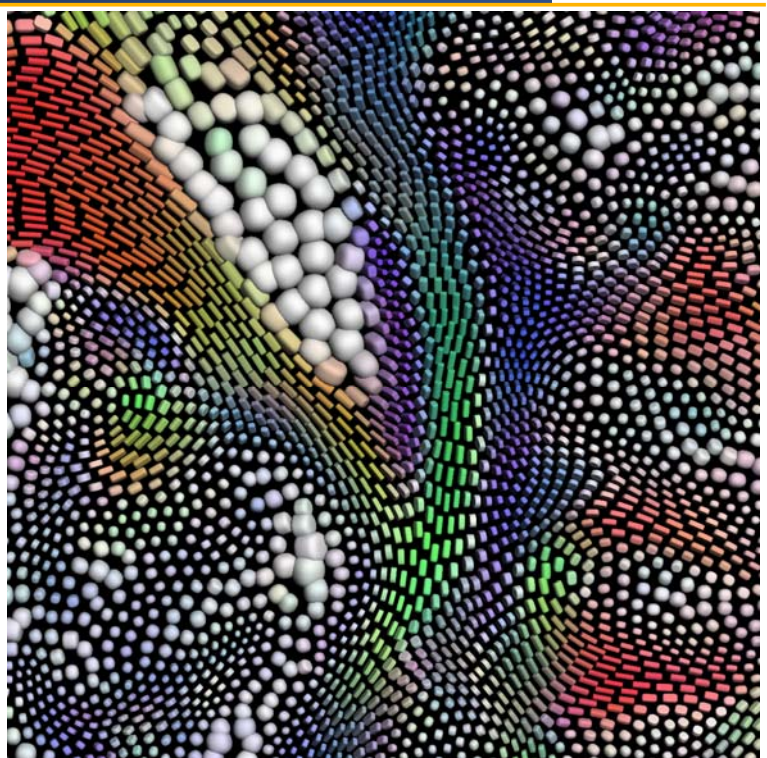


Use particle systems from graphics and anisotropic mesh generation to place glyphs

Avoids visual emphasis on regular grid of original data

Initial evaluation in tumor studies

Kindlmann + Westin Vis '06



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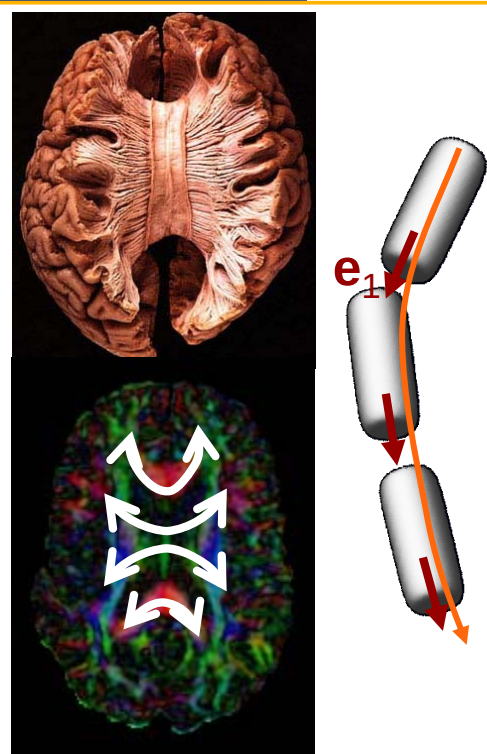
Fiber tractography (Basser 1999)

Path integration along principal eigenvector

Hope: follow paths of individual axons!

- Reality: 2-3 orders of magnitude too coarse

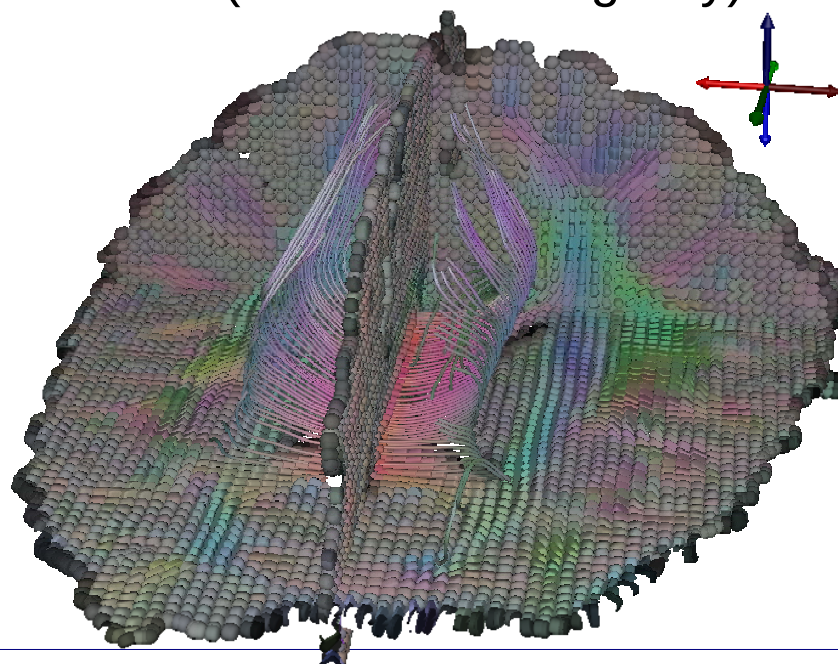
Essentially hyperstreamlines
(Delmarcelle 1993)



- Tensor Field Interpolation/Reconstruction
 - Interpolate in DWIs, tensor coefficients, something else?
 - Noise: smoothing as part of reconstruction (e.g. Zhukov 2002)
- Integration quality, step size
 - Eigensolve at every sample non-trivial
- Seedpoint selection
 - Once per voxel is arbitrary; want proper sampling
- Termination criteria
 - $\text{tr}(\mathbf{D})$ too high or low
 - FA threshold: popular but not robust without mode (CL)
 - Length, # steps, curvature
- Parameter space, Reproducibility, Validation
- What to do at planar anisotropy: stop, coast?

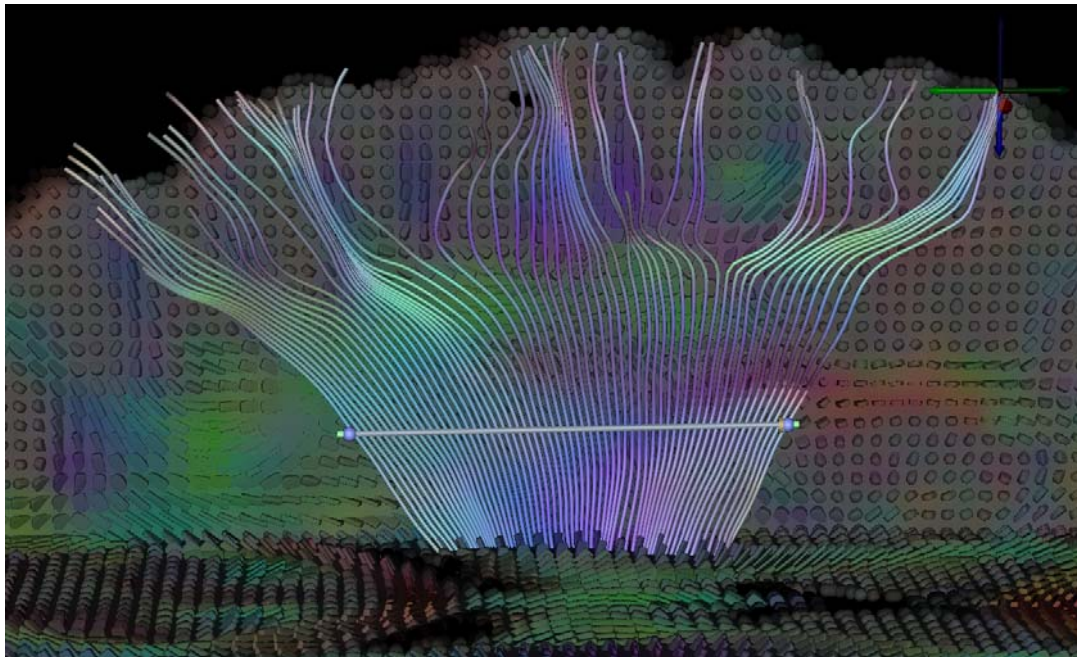
Fiber Tracking: Results

Corpus callosum (seeded mid-sagittally)

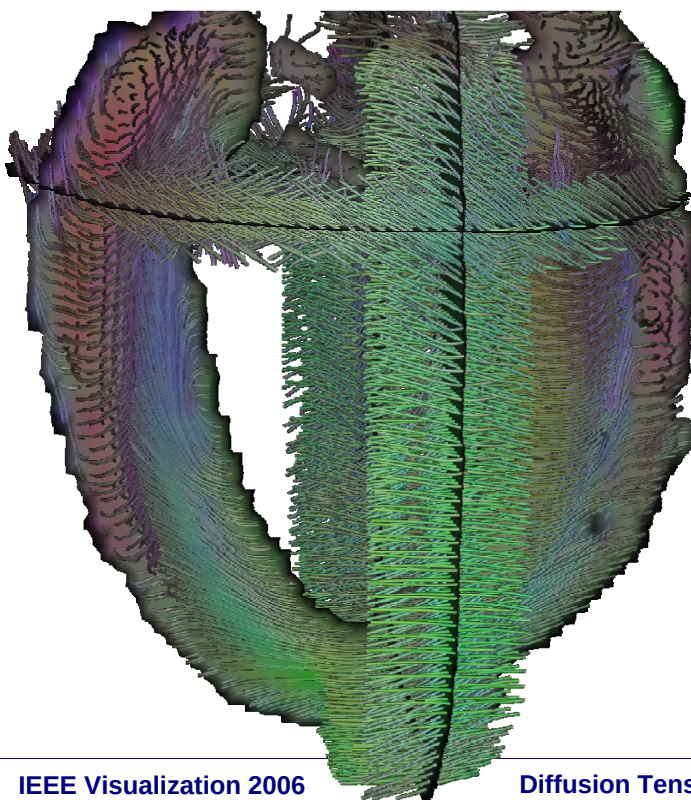


Fiber Tracking: Results

Internal Capsule → Corona Radiata



Fiber Tracking In Heart DT-MRI



Contractile muscle tissue (myofibers) induces anisotropy

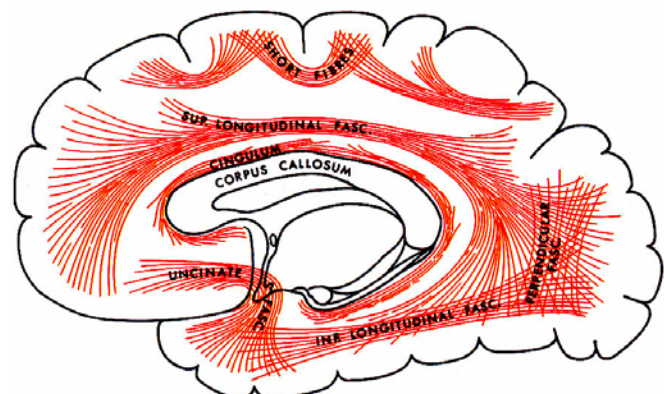
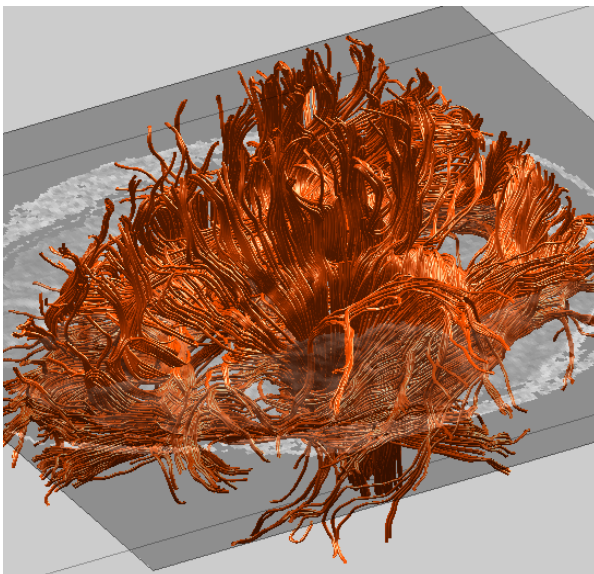
Histological validation (Hsu 1988)

Transmural twist of myofibers

(demo glyphs +
fiber tracking)

Segmentation challenge

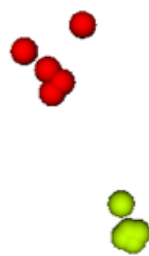
From DT-MRI tractography ...



... to white matter tract models
using **clustering**



Traced fibers



High-dimensional
feature space



Colored bundles

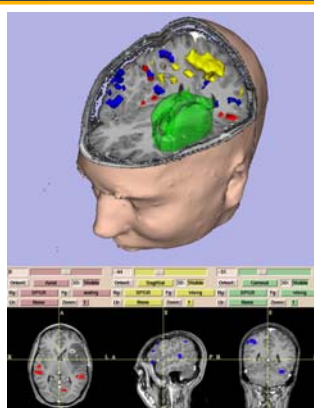
O'Donnell MICCAI 2005

A clustering algorithm takes a number of traced fibers (left), extracts features from these fibers (middle), and produces a segmentation based on the similarity of the fibers (right).

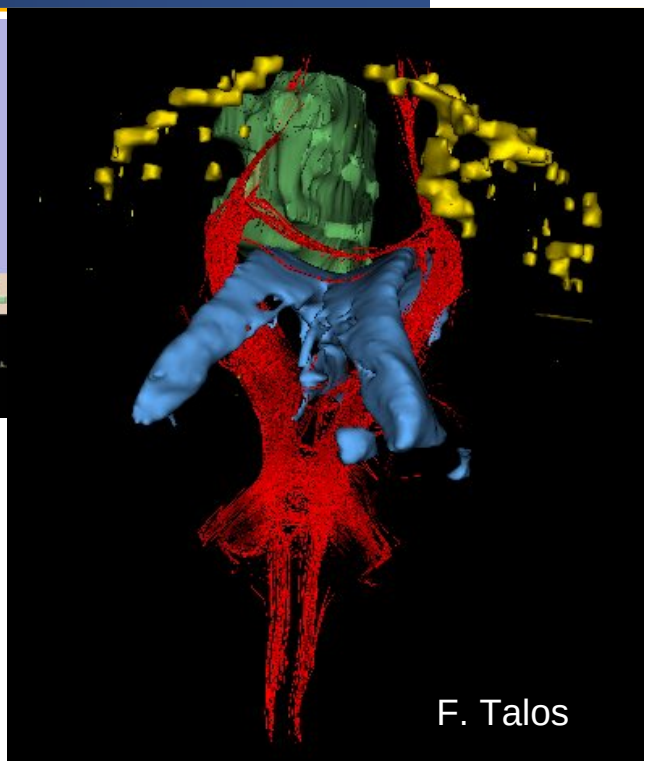
Neurosurgery: tumor study

- 3D Slicer

<http://www.slicer.org>



- Brain connectivity important question
- Relationship between tumor and surrounding white matter



F. Talos

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Future Work Ideas

Interactive fiber generation and analysis

Uncertainty visualization

Bridge between tensor and high-angular DWI

Better use of GPUs

Volume Rendering?

Non-photorealistic rendering?