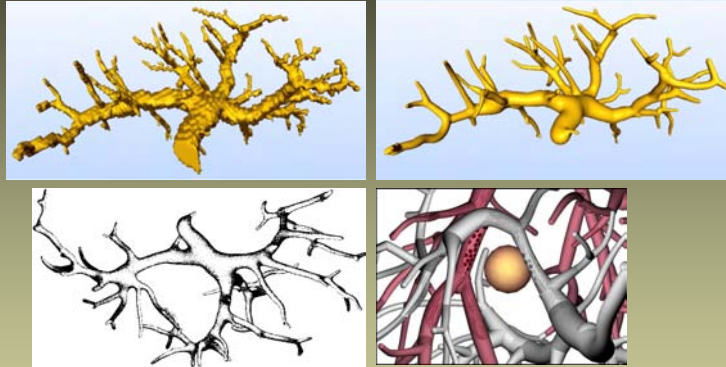


3D Visualization of Vascular Structures



Bernhard Preim, University of Magdeburg, Visualization Research Group

Outline



Methods for 3D Visualization of Vasculature

Model-based Surface Visualization

- Explicit Construction of Vascular Geometries
- Implicit and Parametric Methods

Illustrative Visualization of Vasculature

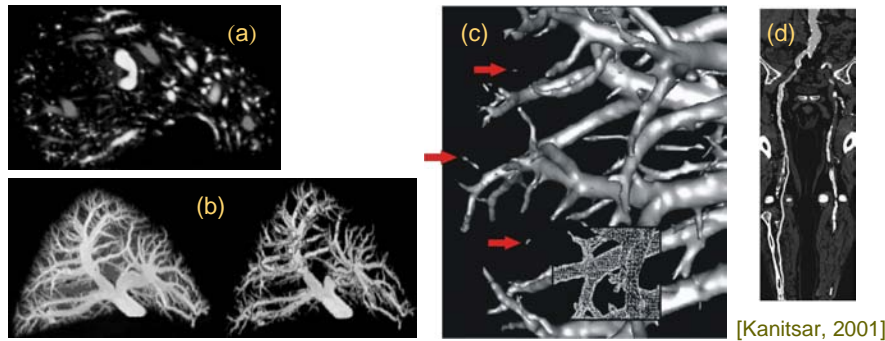
Model-free Surface Visualization

“Traditional” Visualization Approaches



Traditional approaches:

- (a) slice-based examination
- (b) Maximum Intensity Projection, Closest Vessel Projection [Zuiderveld, 1995]
- (c) Isosurface Rendering
- (d) Curved Planar Reformation



Vascular Diagnosis vs. Surgery Planning



Visualization in vascular diagnosis and vascular surgery:

- Close adherence to the image data (vascular cross section)
- Mostly slice-based examination, Curved Planar Reformations
- 3D visualization must be accurate
- Vascular surgery: bypass surgery, endoscopic treatment of aneurysms

Vascular Diagnosis vs. Surgery Planning



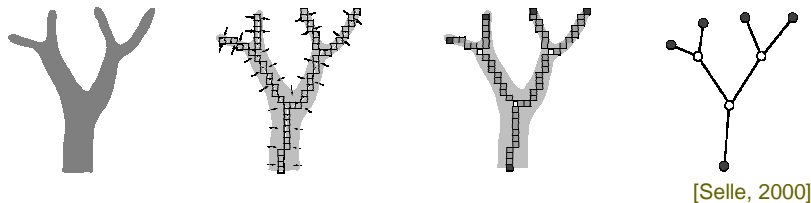
Visualization in surgery planning and medical education:

- Clear communication of topology and morphology
- Comprehension of spatial relations to other structures
- Correct depiction of curvature, depth relations and diminution of the diameter towards the periphery
- Traditional methods not well-suited due to image noise, partial volume effect and limited resolution of CT and MRT
- Reconstruction of vascular structures based on a model

Image Data and Vessel Analysis



High resolution CT- or MR-data → Segmentation → Skeletonization →
Analysis of shape and branching pattern



[Selle, 2000]

Results of vessel analysis:

Graph represents vascular topology

- Edges = branches, nodes = branchings

List of skeleton voxels per branch

Radii per skeleton voxel

Branching information



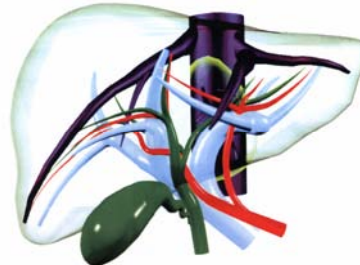
[Ehricke, 1994]

Model-based Visualization – Model Assumption and Requirements



Simplifying model assumption:

- Circular cross-sections of non-pathological vessels
- Keep in mind: methods are not intended for vessel diagnosis



[Mazziotti, 1997]

Requirements:

- Correct representation of the vessel diameter
- Smooth, organic looking vessel shape
- Uniform treatment of all branching types
- Closed vessel ends
- Avoidance of structures inside the vessels

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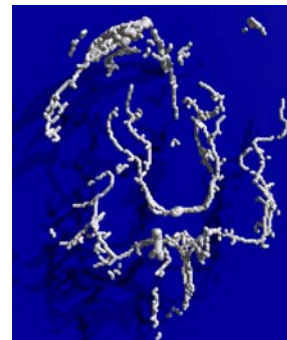
Model-based Visualization – Cylinder Fitting



Gerig et al., 1993: "Symbolic Description of 3d structures applied to cerebral vessel tree obtained from MR angiography volume data".

Graph representation (edges, nodes) of the vessel tree for structural analysis, e.g. identification of subtrees

- Representation of the local vessel diameter by means of fitting cylinders along the vessel skeleton



[Gerig, 1993]

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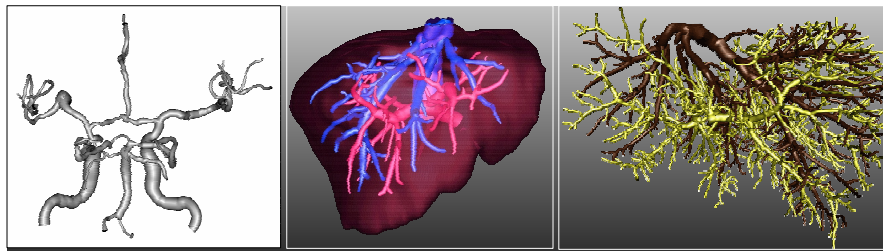
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Model-based Visualization – Truncated Cones Fitting



Filtering: Smoothing of the skeleton and radius (Binominal filter)

Mapping: 1. Concatenation of truncated cones along the skeleton
2. Mapping of truncated cones to polygons



From: Hahn, Preim, Selle (2001)

Left: Cerebral blood vessels (MR-Data: Prof. Terwey, Bremen)

Middle: Hepatic vein and portal vein of clinical dataset (CT-Data: Prof. Galanski, MH Hannover)

Right: Corrosion cast of the human liver (Data: Prof. Fasel, Uni Genf)

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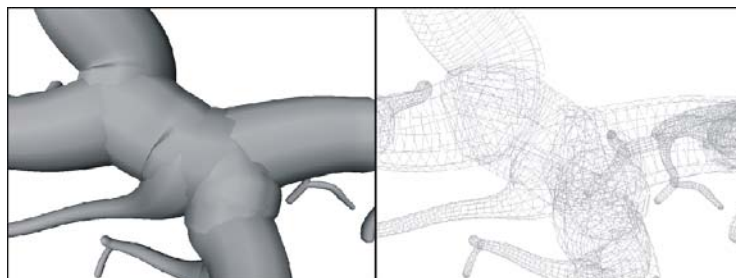
Model-based Visualization – Truncated Cone Fitting



Discontinuities at branchings become obvious at close-up views

Inner polygons arise and therefore not suitable for virtual angiography

But: A very fast method which has been in routine use since 2004 (used for planning ~ 3000 interventions)



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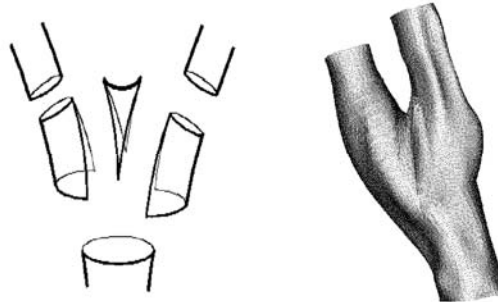
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Model-based Visualization – Freeform Surfaces



Spline-curves represent the vessel skeleton

Voxel ring describes local cross section



[Ehricke, 1994]

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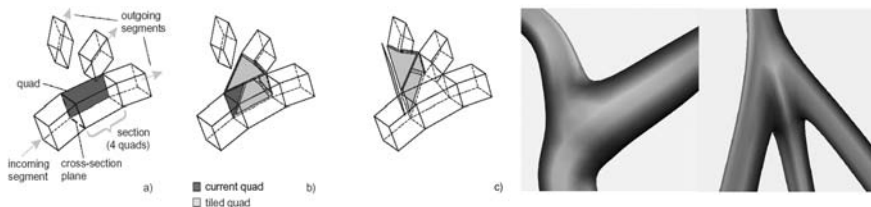
Model-based Visualization – Subdivision Surfaces



Computation of reference frame for each skeleton voxel to avoid twisting of the reconstructed vessel

Visualization in two steps:

- Construction of a coarse initial mesh by means of quads
- Iterative refinement of the initial mesh applying Catmull-Clark subdivision surfaces



[Felkel, 2002]

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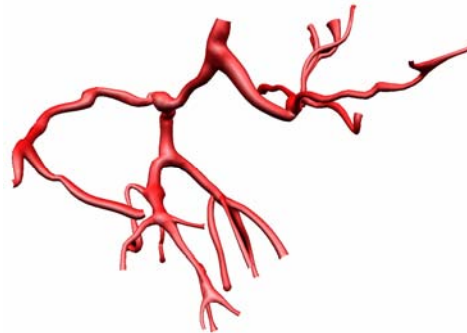
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Model-based Visualization – Subdivision Methods



Enables trade-offs between quality
and speed

High quality at branchings
possible



[Felkel, 2004]

Model-based Visualization – Simplex Meshes



Simplex Meshes: special kind of deformable models [Delingette, 1999]

Each vertex adjacent to 3 neighboring vertices

Visualization in two steps [Bornik, 2005] :

Construction of an initial simplex mesh by connecting adjacent cross-
section polygons

Iterative mesh deformation based on Newtonian law of motion

- External forces and internal regularizing forces

Visualization of Vascular Structures: Implicit Methods

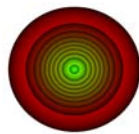


Idea (exploration of implicit surfaces):

Implicit functions ($F(x,y,z) - \text{Iso} = 0$)

Original application in computer graphics

- Blobsy Molecules for the display of electric fields, Blinn [82]



$$F(p) = e^{-\omega x^2}$$

$\omega = \text{width coefficient}$



[Blinn, 1982]

Implicit surfaces for the visualization of tree structures

Energy distribution: skelett points as energy sources

Skelett points define isospheres

Problem: Smooth surfaces at line segments

→ Solution: Convolution Surfaces (Jules Bloomenthal)

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Visualization of Vascular Structures: Convolution Surfaces



Convolution Surfaces (Bloomenthal and Shoemake [1991])

Convolution of a signal with a filter

Here: Convolution of line segments with a 3d-lowpass filter

$$F(p) = \int_s h(s - p) ds = (h \otimes S)(p)$$



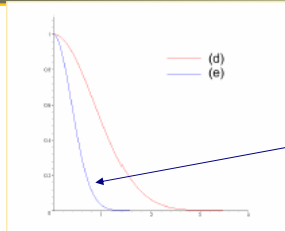
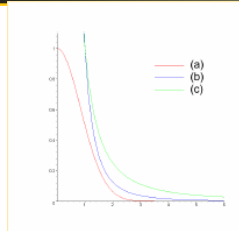
Polygonization with an isovalue depending on the filter

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Visualization of Vascular Structures: Convolution Surfaces



$$h(p) = e^{-d^2/p}, \quad \omega = 5 \ln 2, \quad d > 0$$

$$F(p) = e^{-(r(H)/r(H))^2 \cdot 5 \ln 2} \quad r_{50} = e^{-5 \ln 2} \quad I_{50} = 0$$

$$I_{50} = 1/32 = 0.03125.$$

Exploration of filter functions.

Selection guided by the following criteria:

Correct display of the radius,

Unwanted-Effects,

Fast computation

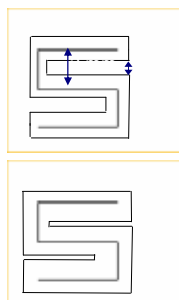
Result: A narrow Gaussian filter is a good choice. For even narrower filter kernels the implicit surface converges against the truncated cone visualization.

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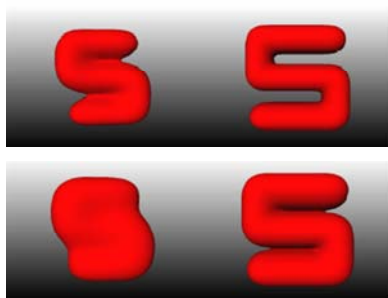
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Visualization of Vascular Structures: Convolution Surfaces



Above: dist.: 3 mm,
radius: 1 mm

Below: radius: 1.37 mm
(3 - 1.37 * 2 = 0.26 mm)



Unwanted Blending

Left: Convolution with „normal“ Gaussian filter

Right: Convolution with narrow Gaussian filter

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Visualization of Vascular Structures: Convolution Surfaces



Studying blending effects by
means of a trifurcation

Blending Strength



Bulging



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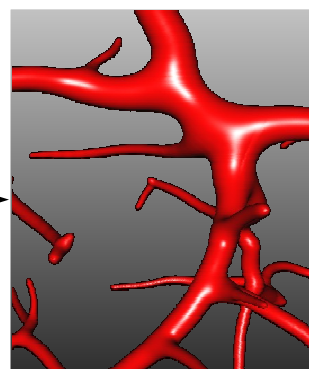
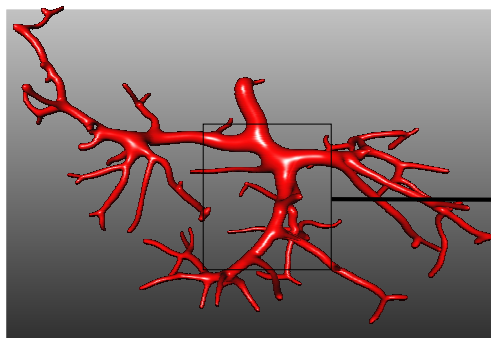
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Visualization of Vascular Structures: Applications of Convolution Surfaces



Portal vein of a human liver



Oeltze/Preim „Visualization of Vascular Structures with
Convolution Surfaces“, IEEE Transactions on Medical
Imaging

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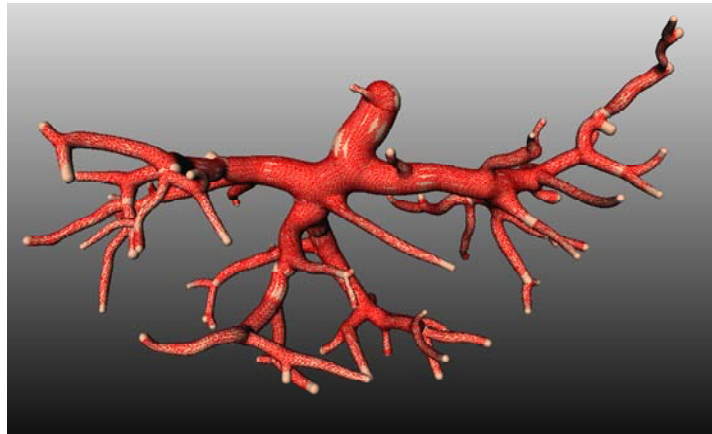
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Visualization of Vascular Structures: Validation of Convolution Surfaces



Comparison: Convolution surface as wireframe; truncated cones as shaded surface visualization.

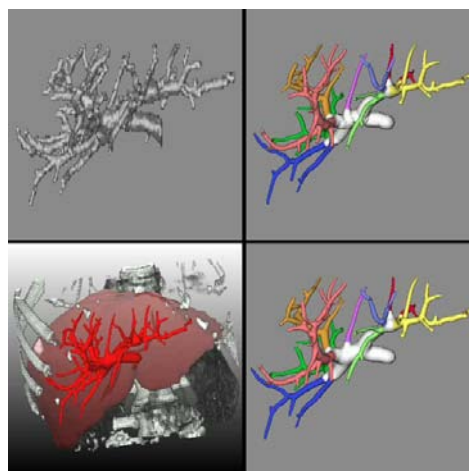


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Visualization of Vascular Structures: Validation of Convolution Surfaces



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Visualization of Vascular Structures: Validation of Convolution Surfaces



Quantitative validation (directional distances) between CS and Truncated Cones and CS to Isosurface of the segmentation result.

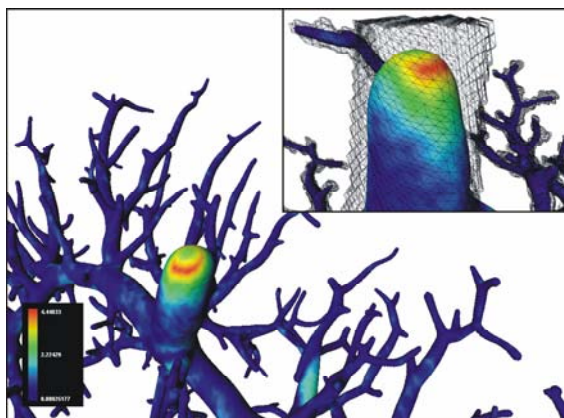
Distances strongly depend on the width coefficient. Measurements with the following filter:

$$F(p) = e^{-(r(H)/r(H))^2 5 \ln 2} - I_{SO} = e^{-5 \ln 2} - I_{SO}$$

Results:

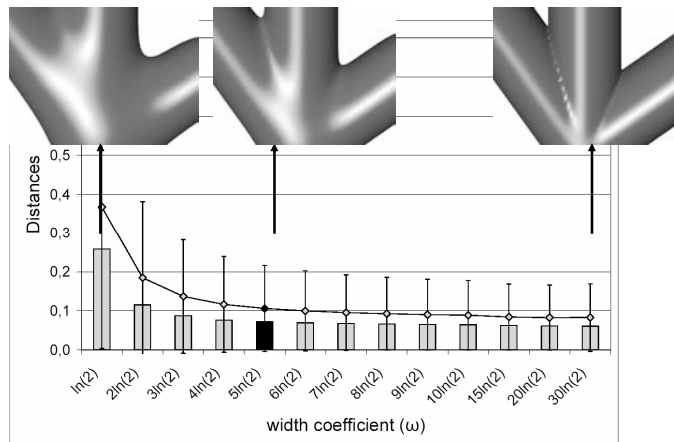
- Quantitative visualization (color coding)
- Histogrammes of distances
- Statistic Evaluation (mean, standard deviation, ...)

Visualization of Vascular Structures: Validation of Convolution Surfaces



CS → Isosurface: Large distances only at the root of vascular trees

Visualization of Vascular Structures: Validation of Convolution Surfaces



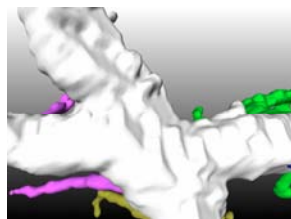
Width Coefficient versus accuracy (average and standard deviation of directional distances to isosurface)

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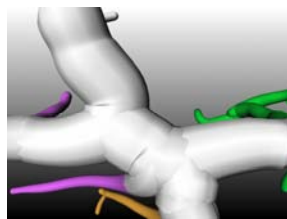
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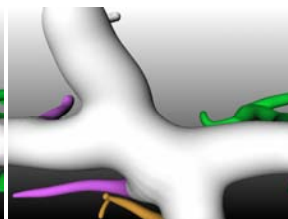
Visualization of Vascular Structures: Evaluation of Convolution Surfaces



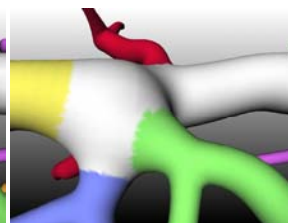
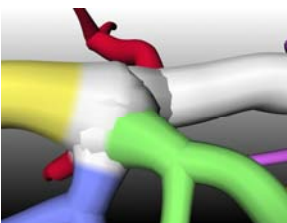
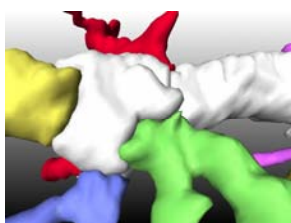
Isosurface of the
segmentation result



Truncated Cones



Convolution Surfaces



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Visualization of Vascular Structures: Evaluation of Convolution Surfaces



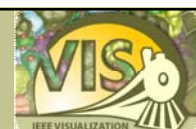
Method	Clarity (n=11)		Comprehensibility (n=11)		Similarity to operative Views (n=8)		Visual Quality (n=11)	
	\bar{O}	σ	\bar{O}	σ	\bar{O}	σ	\bar{O}	σ
Iso	1.8	0.69	1.9	0.85	1.6	0.7	1.7	0.69
Cones	3.7	0.84	3.9	0.86	3.5	0.9	3.8	0.71
CS	4.1	0.87	4.1	0.89	4.0	0.89	4.2	0.76

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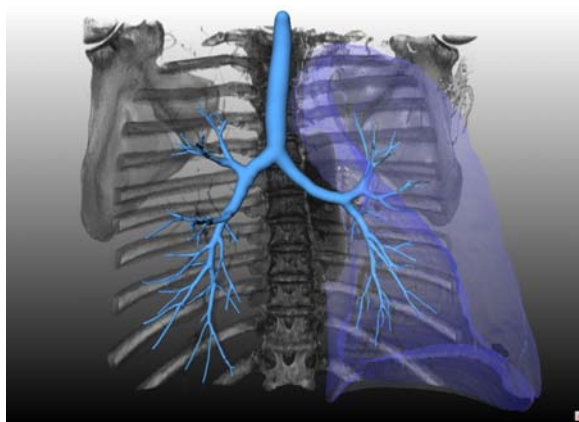
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Application Scenarios – Analysis of the Bronchial Tree



Bronchial tree (> 3000 branchings, > 3 M triangles, 54 seconds)
in a human lung (volume rendering).



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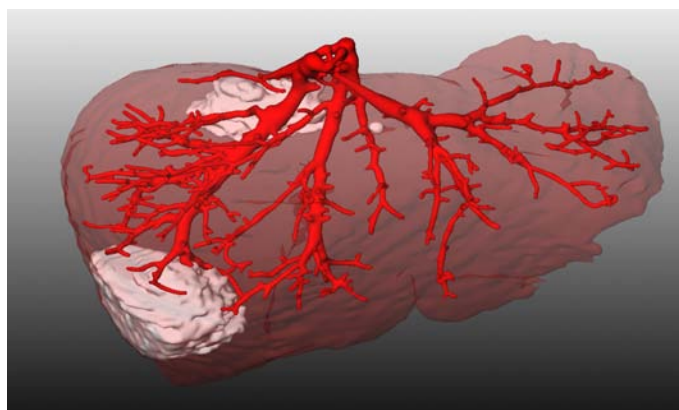
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Application Scenarios – Tumor Resection (1)



Visualization of the portal vein inside a human liver
(with three tumors).

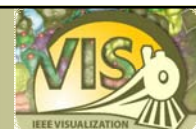







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Model-based Visualization – Comparison



Method	Geometry					
Gerig, 1993	Cylinder	no local diminution	no	yes	no	no
Hahn, 2001	Truncated cone	Yes	No	yes	yes	no
Ehricke, 1994	Freeform Surfaces	yes*	yes*	no*	no*	yes*
Felkel, 2002	Subdivision Surface	Yes	Yes	yes	no	yes
Bornik, 2005	Simplex Mesh	yes	Yes	yes	yes	yes
Oeltze, 2004	Convolution Surface	yes	yes	yes	yes	yes

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Illustrative Visualization of Vasculature

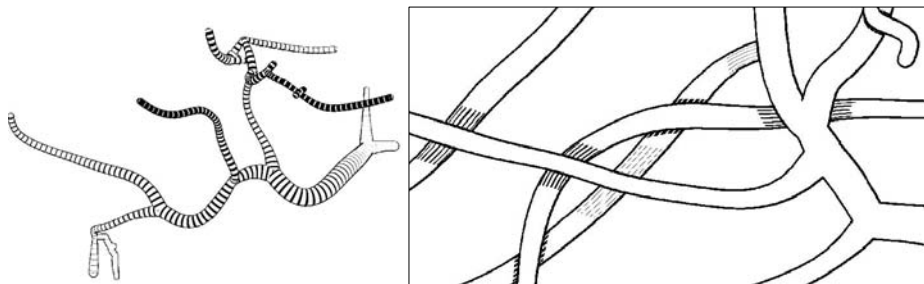


Intraoperative projection of vasculature on liver surface

Visualization of distance information by means of procedural textures

Visualization method: truncated cones

[Ritter et al. 2006]



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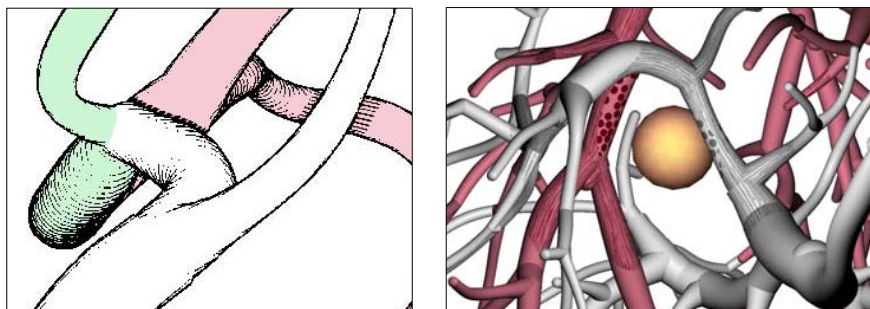
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Illustrative Visualization of Vasculature



Visualization of surface orientation by means of hatching

Varying textures to code distances between structures



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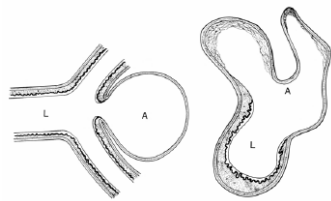
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Model-Free Visualization

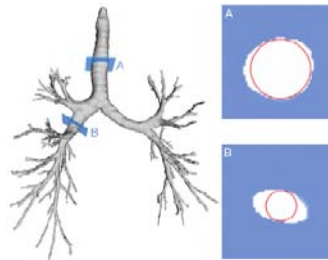


Simplifying model-assumption of circular cross-sections is invalid for pathologic vessel parts, e.g. aneurysms

Even Non-pathologic vessels may exhibit non-circular cross-sections



[Osborn, 1999]



[Schumann, 2006]

Model-Free Visualization – Multi-level Partition of Unity Implicits



Approximation of a point cloud by a surface [Ohtake et al. 2003]

Visualization of vasculature based on post processed segmentation result (points placed within boundary voxels)

Arbitrary cross-sections may be reconstructed

Suitable for vessel diagnosis

Algorithm:

- Spatial subdivision of the point cloud by an ctree
- Local approximation by means of surfaces
- Blending of local approximations results in global approximation

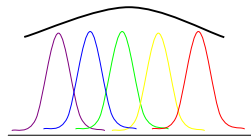
Multi-level Partition of Unity Implicits



Adaptive refinement



Piecewise quadratic local approximation



- Fast reconstruction of surfaces from scattered data
- Surface approximation with adaptive error control
- Search for points in spherical regions

[Ohtake et al. 2003]



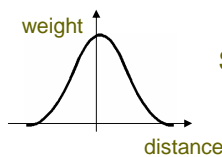
Approximation with 14 million points

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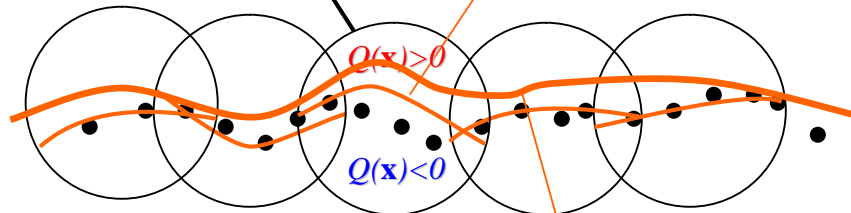
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Model-Free Visualization Partition of Unity



Support of $Q(\mathbf{x})$

$Q(\mathbf{x})=0$ (local approximation with quadrics)



Weighted average of local approximations

$$f(\mathbf{x}) = \frac{\sum w_i(\mathbf{x}) Q_i(\mathbf{x})}{\sum w_i(\mathbf{x})}$$

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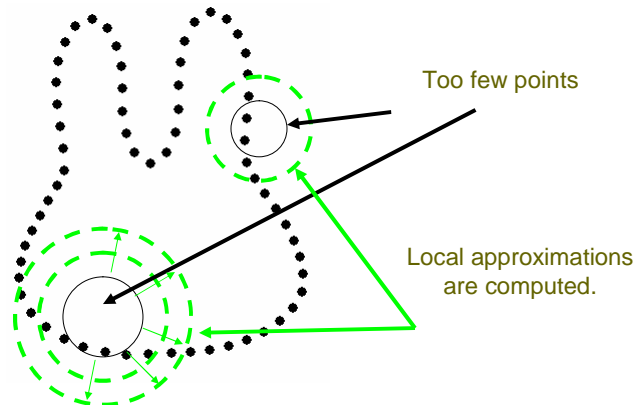
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Local Approximations



If not enough points are in the local region \rightarrow expand it.

Parameter: Maximum octtree depth, initial size of the region, growth factor



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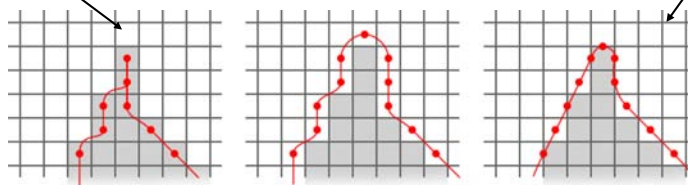
Model-Free Visualization



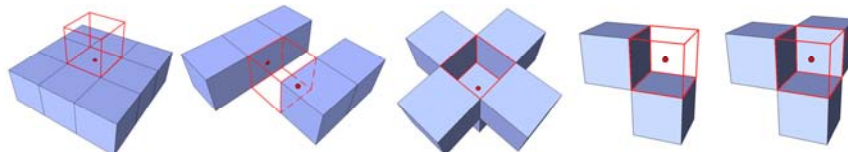
Border voxels as initial places for points

Degenerating of thin vessels

Ideal point distribution



Different cases for placing points



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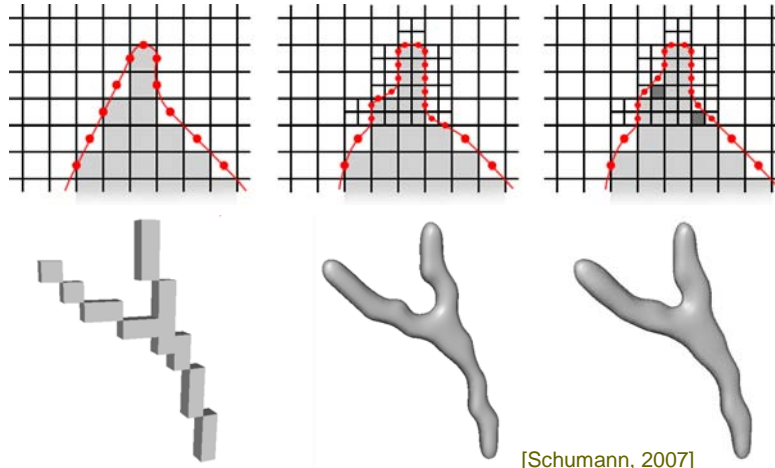
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Model-Free Visualization



Adaptive subsampling of thin branches



[Schumann, 2007]

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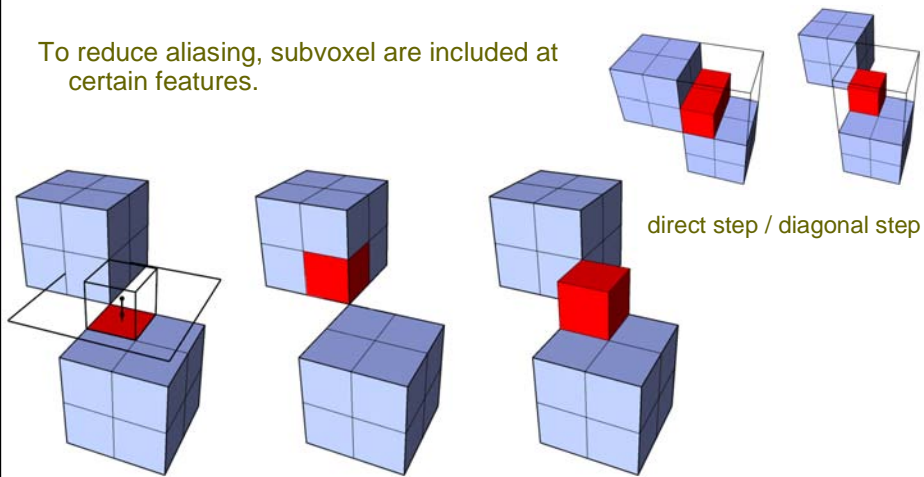
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Model-Free Visualization



To reduce aliasing, subvoxel are included at certain features.



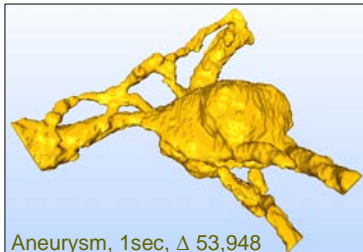
[Schumann, 2007]

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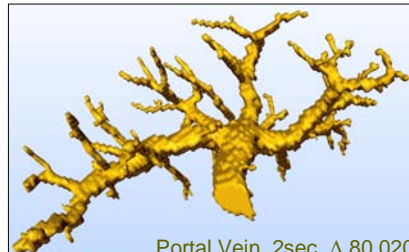
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Model-Free Visualization – Results (1)

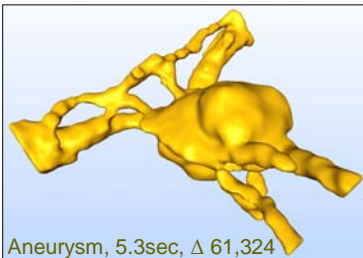


Aneurysm, 1sec, Δ 53,948

MC

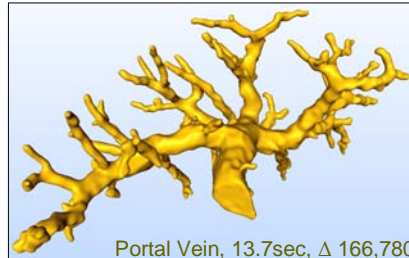


Portal Vein, 2sec, Δ 80,020



Aneurysm, 5.3sec, Δ 61,324

MPU



Portal Vein, 13.7sec, Δ 166,780

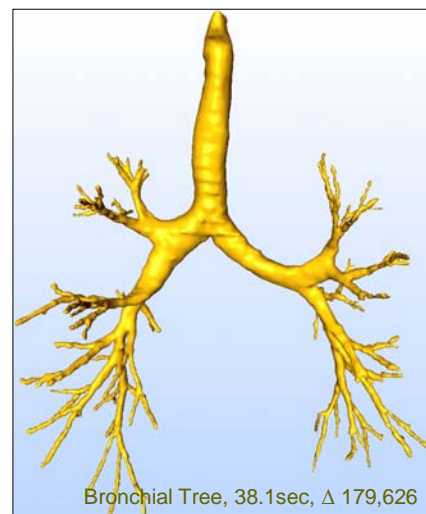
[Schumann, 2007]

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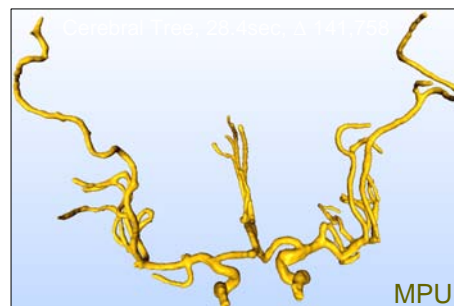
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Model-Free Visualization – Results (2)

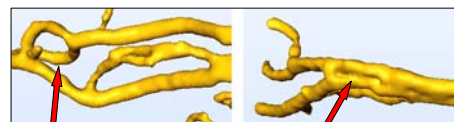


Bronchial Tree, 38.1sec, Δ 179,626



MPU

[Schumann, 2007]



Cycle

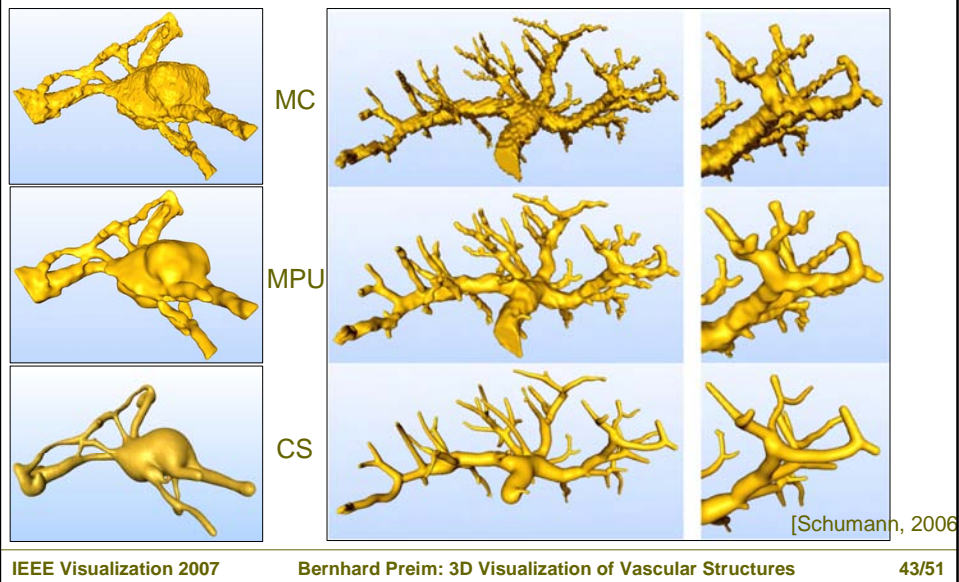
Adjacent Vessels

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Model-Free Visualization – Results (3)



Model-Free Visualization – Smoothness



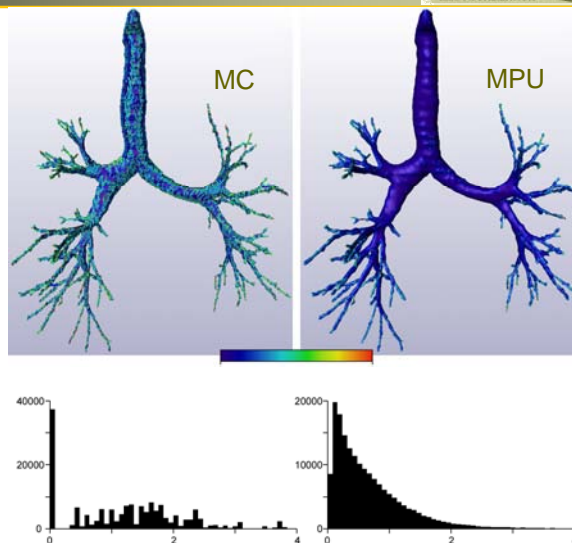
Maximum curvature as a measure of smoothness

Computed using AMIRA™

Comparison of MC and MPU

Histogram of the curvature values

[Schumann, 2006 und 2007]



Model-Free Visualization – Surfaces Distances



Surface distances from MC- to MPU-result in voxel diagonals (V_d)

Dataset	Φ	σ	Rms	Median	Max	$>V_d/2$ [%]
Bronchial Tree	0.17	0.11	0.21	0.16	1.4	0.69
Portal Vein	0.17	0.11	0.2	0.15	0.84	0.82
Cerebral Tree	0.2	0.13	0.24	0.2	1.68	1.7
Aneurysm	0.21	0.16	0.27	0.19	1.9	4.1
Average	0.19	0.13	0.23	0.17	1.46	1.84

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Conclusion



Therapy planning and medical education require clear communication of topology and morphology

Model-based reconstruction of the vascular surface

- *Subdivision* and *Convolution Surfaces* closely adhere to the data and generate smooth, organic looking surfaces

!!! Not suitable for vessel diagnosis due to simplifying model assumption of circular cross-sections

Vessel diagnosis requires accurate representation of vascular cross-section

Model-free reconstruction of the vascular surface directly from the segmentation result by means of MPUs

!!! Suitable for vessel diagnosis since no model assumption is made

Quantitative analysis of global/local deviations for validation

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Future Work



Accelerating the visualization with Convolution Surfaces and MPUs to facilitate an application in clinical routine

Hybrid visualization, integrating Convolution Surfaces and MPUs for vessel parts with nearly circular cross-sections and for vessel parts whose cross-sections strongly deviate from this model assumption, respectively

Mapping of additional information to the vascular surface, e.g. existence of plaque or blood flow quantities

Adapting general methods to specific needs, e.g., exploration of the cardiovascular system

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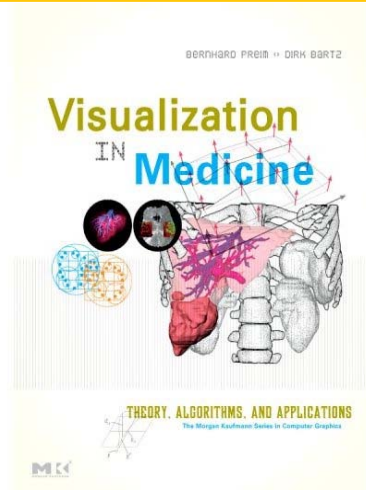
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